

Name:

ID Number:

Exam Number:

Grade: 1: ... 2: ... 3: ... 4: ... 5: ... 6: ... 7: ... 8: ... Total:

SOLVE ALL the problems IN THE SPACE PROVIDED

Read the Problems CAREFULLY!

THERE ARE 6 (SIX) PAGES THIS PAGE INCLUDED

In the exam, the following matrices MAY be used. Do not get puzzled if a reference to matrix X , Y or Z or etc arises! No problem modifies X, Y, Z, R, S in a way that missing that problem would change the answer of any other problem of the exam.

If you are asked to evaluate a MATLAB expression, and you think the result would generate an ERROR because a variable is undefined you could write **ERROR** instead of giving an answer. For example `five == 5` generates an **ERROR** since variable `five` is never defined anywhere in the exam.

$$X = \begin{bmatrix} 2 & 1 & 2 & 1 \\ 2 & 3 & 3 & 2 \\ 3 & 4 & 4 & 3 \end{bmatrix}, Y = \begin{bmatrix} 1 & 1 & 2 \\ 2 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, Z = [1 \ 2 \ 1 \ 2], R = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, S = [1 \ 2 \ 3].$$

Problem 1. (48 POINTS)

Give short answers to the following questions.

- (1) How many bytes in 1KiB?
- (2) What is an 1Kb?
- (3) How many bytes is a MATLAB `double`?
- (4) How many bytes is a MATLAB `uint16`?
- (5) How many bytes is a MATLAB `logical`?
- (6) What is the range of values for `int8` in MATLAB? (give number of values, lowest and highest value in the range.)
- (7) What is array element $Y(\text{end} - 1, \text{end} - 1)$?
- (8) What is array element $X(\text{end} - 3)$?
- (9) Represent decimal (i.e. base-10) integer 49 in hexadecimal.
- (10) How many bits in a byte nowadays?
- (11) How much is $j * j$ in MATLAB?
- (12) Represent decimal (i.e. base-10) integer 49 in binary.

Problem 2. (30 POINTS)

What is the **value**, **Size** (i.e geometry/shape), number of **Bytes**, and the **Class** (i.e. data type) of variables `p2a`, `p2b`, `p2c`, `p2d`, `p2e`, `p2f`, as needed for the MATLAB program below.

```
>> clear
>> p2a = 5 < 5 < 5;
>> p2a
>> whos p2a          %p2a= ..... Size ... x ... Bytes ..... Class .....
>> p2b = int8(5 < 5);
>> p2b
>> whos p2b          %p2b= ..... Size ... x ... Bytes ..... Class .....
>> p2c = 5 == 5 + 5;
>> p2c
>> whos p2c          %p2c= ..... Size ... x ... Bytes ..... Class .....
>> p2d = int32(5 * 5 - 10/ 5);
>> p2d
>> whos p2d          %p2d= ..... Size ... x ... Bytes ..... Class .....
>> p2e = 11:-2:1;
>> p2e
>> whos p2e          %p2e= ..... Size ... x ... Bytes ..... Class .....
>> p2f = transpose(R)*R;
>> p2f
>> whos p2f          %p2f= ..... Size ... x ... Bytes ..... Class .....
```

Problem 3. (60 POINTS)

Evaluate the following MATLAB expressions.

(example) $z = \text{ones}(2)$ **Answer** $z = [1 \ 1; 1 \ 1]$.

```
>> clear;
>> p3a = 2:3:10
>> p3a

>> p3b = size(X);
>> p3b

>> p3c =length(X);
>> p3c

>> p3d = 2*eye(3)+ones(3)+1;
>> p3d

>> p3e = sum(X);
>> p3e

>> p3f = diag(X);
>> p3f

>> p3g = X(end, 2:end);
>> p3g

>> p3h = Y .* transpose(Y);
>> p3h

>> p3i = diag(diag(X));
>> p3i

>> p3j = sum(X(:));
>> p3j

>> p3k = transpose(S) * S;
>> p3k

>> p3l = S *R ;
>> p3l

>> p3m = S* transpose(S);
>> p3m

>> p3n = 2:-1:2;
>> p3n

>> p3o = length('1234');
>> p3o
```

Problem 4. (16 POINTS)

For **p3k**, **p3m** of Problem 3 provide the following information.

```
>> p3k;
>> whos p3k           Size ... x ... Bytes ..... Class .....
>> p3m;
>> whos p3m           Size ... x ... Bytes ..... Class .....
```

Problem 5. (24 POINTS)

(a) List the elements of Y in column-major order/filin/form.

(b) List the elements of Y in row-major order/filin/form.

Problem 6. (24 POINTS)

(a) Write MATLAB code that copies matrix X into matrix B .

Write MATLAB code that uses the colon operator and extracts/prints

(b) the second column of B ,

(c) the second row of B , and

(d) deletes from B its second row

(e) prints X in column major form in the form of a column,

(f) that defines row vector $[4, 9, 16, 25, 36, \dots, 256]$ in as short a way as possible (fewer than 15 characters).

(a)

(b)

(c)

(d)

(e)

(f)

Problem 7. (24 POINTS)

What is the value of $p7a$, $p7b$, $p7c$, $p7d$, $p7e$, $p7f$ after the execution of the following code?

```
>> p7a=10;
>> p7b=20;
>> p7c=0;
>> p7c=p7a;
>> p7a=p7b;
>> p7b=p7c;
>> p7a          % p7a = .....
>> p7b          % p7b = .....
>> p7c          % p7c = .....
```

```
>> p7d=10;p7e=5; p7f=5;
>> p7d= p7d+p7e+p7f;
>> p7e= p7d+p7f;
>> p7f= p7d+p7e+p7f;
>> p7d          % p7d = .....
>> p7e          % p7e = .....
>> p7f          % p7f = .....
```

Problem 8. (24 POINTS)

The following code resides in a file named `compute.m`. Apparently it attempts to compute $e = \exp(1.0)$ using the approximation

$$e = 1 + \frac{1}{1!} + \frac{1}{2!} + \dots + \frac{1}{n!}$$

implied by the Taylor expansion of $\exp(x)$ for $x = 1$. However the code is incomplete. The code uses function `cumprod()`. This computes the cumulative products of the elements of say vector x . Thus if $x = [2 \ 3 \ 4]$, then `cumprod(x) = [2 \ 6 \ 24]`. We ask you to fill the incomplete lines (Lines 5 and 6) to turn this into a correct MATLAB M-file for this computation/approximation of e . Line 7 prints the approximation of e to the desired precision/order.

```
% Compute e approximation to order n           Comment Line 1
n = input('Order of approximation ');         % Line 2
a = [1 1:n] ;                                  % Line 3
a = cumprod(a) ;                               % Line 4
b = ;                                           % Line 5
c = ;                                           % Line 6
disp(c) ;                                       % Line 7
```

THIS IS THE END OF PAGE 5 CONTAINING PROBLEM 8. TURN PAGE.

$$X = \begin{bmatrix} 2 & 1 & 2 & 1 \\ 2 & 3 & 3 & 2 \\ 3 & 4 & 4 & 3 \end{bmatrix}, Y = \begin{bmatrix} 1 & 1 & 2 \\ 2 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, Z = [1 \ 2 \ 1 \ 2], R = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, S = [1 \ 2 \ 3].$$

This is the last page (Page 6) of the exam.

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You may tear-off this last page and use it as scratch paper; do not turn IT in

End of Exam 1